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# ***Typing migration-control in $Isd\pi$***

Francisco Martins

DI/FCUL

**Joint work with**

António Ravara

# *Lexically Scoped Distributed* $\pi$

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- ⑥ Extends  $\pi$ , distributing processes over networks of named sites where they compute.
- ⑥ Processes allowed to:
  - △ communicate via channels (as in  $\pi$ ), but only locally
  - △ migrate from site to site.

# Main concepts

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In  $lsd\pi$

- ⑥ channels are
  - △ resources associated *uniquely* to sites
  - △ located at *creation* time
    - In  $s[(\nu c) \dots]$ , channel  $c$  is created *locally*, at  $s$ ;
    - In  $r[(\nu c@s) \dots]$ , channel  $c$  is created *remotely*, to be located at  $s$ ;

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    - In  $r[(\nu c@s) \dots]$ , channel  $c$  is created *remotely*, to be located at  $s$ ;
- ⑥ sites are
  - △ *collections* of channels;
  - △ *shells* of local computations.

# *lsd* $\pi$ **by example**

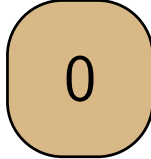
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r  
 $a@s! \langle b \rangle$

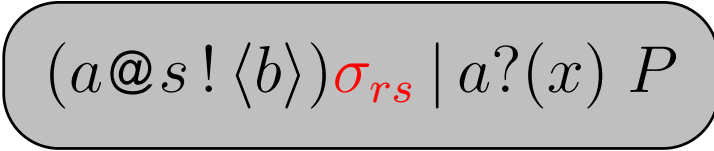
s  
 $a?(x) P$

$r[a@s! \langle b \rangle] \parallel s[a?(x) P]$

# *lsd* $\pi$ **by example**

$r$   
0

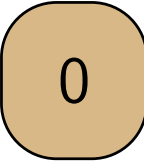
$s$

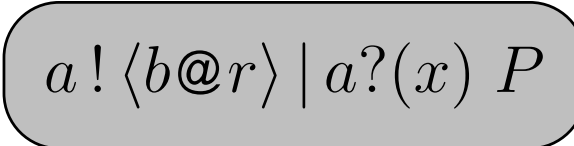
 $(a@s! \langle b \rangle) \sigma_{rs} \mid a?(x) P$

$r[a@s! \langle b \rangle] \parallel s[a?(x) P]$

↓

$r[0] \parallel s[(a@s! \langle b \rangle) \sigma_{rs} \mid a?(x) P]$

$r$   


$s$   


$r[a@s! \langle b \rangle] \parallel s[a?(x) P]$

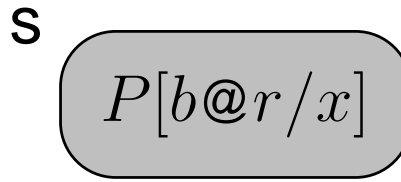
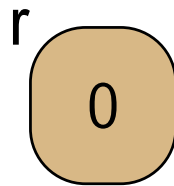
↓

$r[0] \parallel s[(a@s! \langle b \rangle) \sigma_{rs} \mid a?(x) P]$

||

$r[0] \parallel s[a! \langle b@r \rangle \mid a?(x) P]$

# *lsd* $\pi$ **by example**



$$r[a@s! \langle b \rangle] \parallel s[a?(x) P]$$



$$r[0] \parallel s[(a@s! \langle b \rangle) \sigma_{rs} \mid a?(x) P]$$

||

$$r[0] \parallel s[a! \langle b@r \rangle \mid a?(x) P]$$



$$r[0] \parallel s[P[b@r/x]]$$



⑥ Lexically Scoping Distribution:

**what you see is what you get!**

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## ⑥ a flavour ...

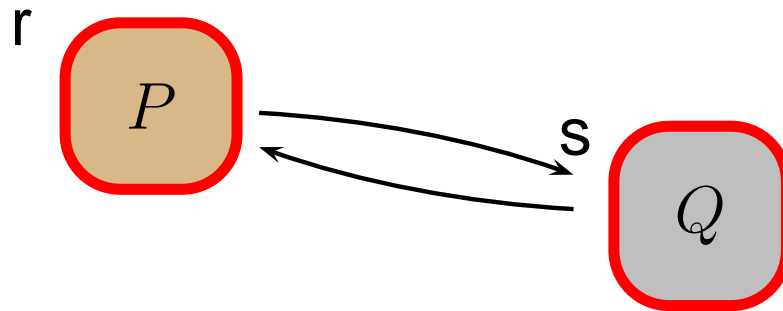
$$(\nu a@s) r_{G_1}[a@s! \langle b \rangle] \parallel s_{G_2}[a?(x : S) P]$$

∴ simple names are local;

remote names are explicitly located;

# Aim of this work

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- ⑥ Ensuring security policies: sites allowed to
  - △ send messages (remote communicating)
  - △ migrate processes
  - △ create remote names

## 6 Processes

$$P, Q ::= 0 \mid u! \langle v \rangle \mid u?(x : S) P \mid P \mid Q \mid (\nu u) P$$

simple channels	$a, b, c, x, y$	channels	$u, v$	$::= a \mid a@s$
sites	$r, s, t$	set of sites	$R, S$	

## 6 Processes

$$P, Q ::= 0 \mid u! \langle v \rangle \mid u?(x : S) P \mid P \mid Q \mid (\nu u) P$$

## 6 Networks

$$N, M ::= 0 \mid s_G \mathbf{[P]} \mid N \parallel M \mid (\nu a@s) N$$

simple channels  $a, b, c, x, y$  channels  $u, v ::= a \mid a@s$   
sites  $r, s, t$  set of sites  $R, S$   
 $G?$  stay tuned ...

# Syntax (types)

---

$\Gamma ::= \{s_1 : (\varphi_1, G_1), \dots, s_n : (\varphi_n, G_n)\}$  typings

$\varphi ::= \{a_1 : \gamma_1, \dots, a_n : \gamma_n\}$  site types

$G ::= \{\text{rem} : S_1, \text{mig} : S_2, \text{new} : S_3\}$  site policies

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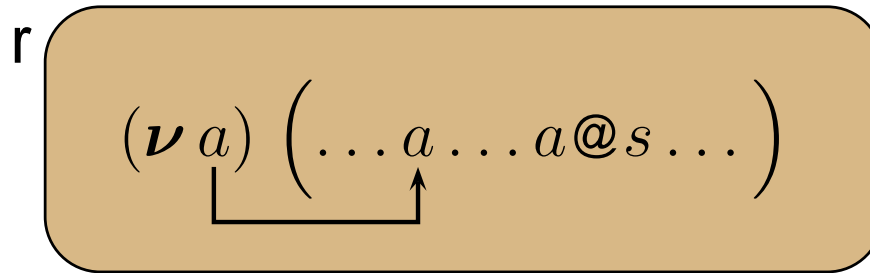
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$\gamma ::= \text{ch}(\gamma)@S^t \mid \text{val}$  channel types

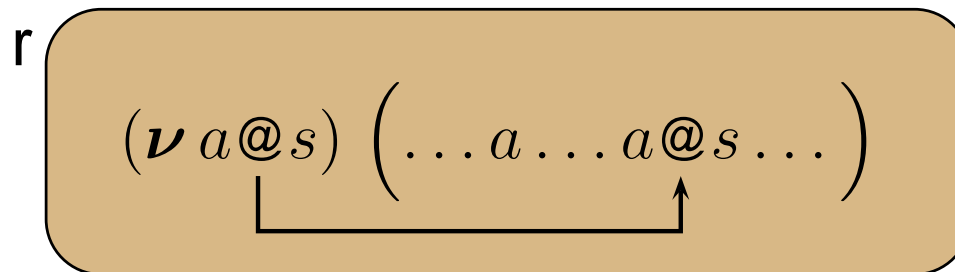
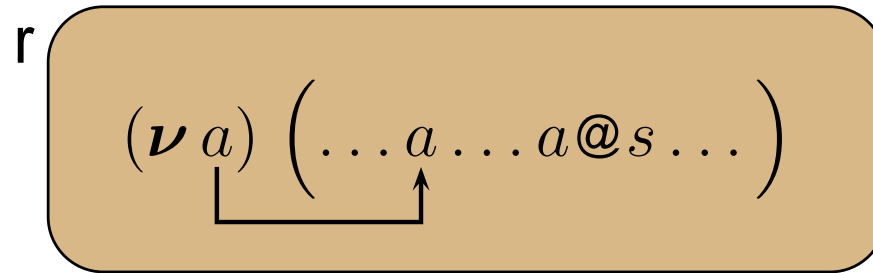
$t ::= o \mid i \mid b$  site tags

# Free names

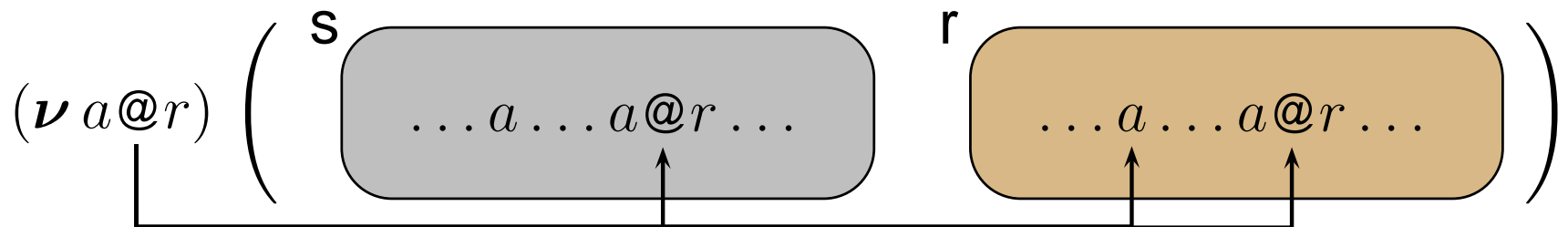
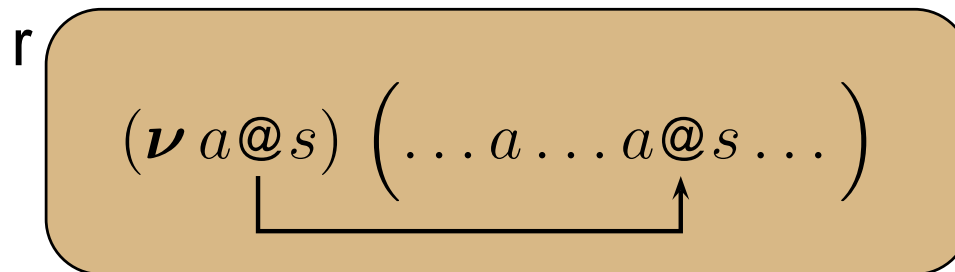
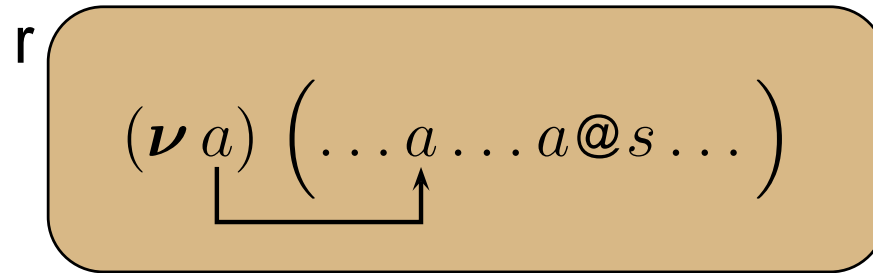




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# ***Structural congruence (some rules)***

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$$(\nu a@s) s_G[P] \equiv s_G[(\nu a@s) P] \quad a \notin \text{fn}(P)$$

⑥ Example:

$$(\nu a@s) s_G[a! \langle b \rangle \mid a@s! \langle c \rangle] \not\equiv s_G[(\nu a@s) a! \langle b \rangle \mid a@s! \langle c \rangle]$$


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# Reduction rules (some rules)

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$$s_G[a! \langle v \rangle \mid a?(x : S) P] \rightarrow P[v/x]$$

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$$s_G[a! \langle v \rangle \mid a?(x : S) P] \rightarrow P[v/x]$$

$$\begin{aligned} s_{G_1}[P] \parallel r_{G_2}[a@s?(x : S) Q] \\ \rightarrow s_{G_1}[P \mid (a@s?(x : S) Q)\sigma_{rs}] \parallel r_{G_2}[0], \quad r \neq s \end{aligned}$$

$\sigma_{rs}$  translates free names from  $r$  to  $s$ :

$$\begin{aligned} \sigma_{rs}(s) &= s & \sigma_{rs}(a@s) &= a \\ \sigma_{rs}(a) &= a@r & \sigma_{rs}(a@t) &= a@t, \quad t \notin \{r, s\} \end{aligned}$$



# Security policies violation

---

Let  $r \neq t$

⑥ Remote communication

$$s_{\{\text{rem}:\{t\}\}}[P] \parallel r_{G_1}[a@s! \langle x \rangle]$$

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$$\mathcal{S}_{\{\text{rem}:\{r\}\}}[a?(x : \{t\}) 0] \parallel r_{G_1}[a@s! \langle b@r \rangle]$$

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Let  $r \neq t$

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$$s_{\{\text{mig}:\{t\}\}}[P] \parallel r_{G_1}[a@s? (x : S) Q]$$

# Security policies violation

Let  $r \neq t$

- ⑥ Remote communication
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$$S_{\{\text{mig}:\{t\}\}}[P] \parallel r_{G_1}[a@s?(x : S) Q]$$

$$S_{\{\text{rem}:\{r\}\}}[a?(x : \{r, t\}) x! \langle c \rangle] \parallel r_{\emptyset}[a@s! \langle b \rangle]$$

# Security policies violation

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Let  $r \neq t$

- ⑥ Remote communication
- ⑥ Migration
- ⑥ Name creation

$$s_{\{\text{new}:\{t\}\}}[P] \parallel r_{G_1}[(\nu a@s) Q]$$

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- ⑥ Migration
- ⑥ Name creation

$$s_{\{\text{new}:\{t\}\}}[P] \parallel r_{G_1}[(\nu a@s) Q]$$

$$(\nu a@s) s_{\{\text{new}:\{r\}\}}[P] \parallel r_{G_1}[a@s! \langle b \rangle] \parallel t_{G_2}[a@s! \langle c \rangle]$$

# Subtyping relation

$$b \leq i \quad b \leq o$$

$$\frac{R \subseteq S}{S^o \leq R^o} \quad \frac{S \subseteq R}{S^i \leq R^i} \quad \frac{t \leq t'}{S^t \leq S^{t'}}$$

$$\gamma \leq \gamma \quad \frac{\gamma_1 \leq \gamma_2 \quad \gamma_2 \leq \gamma_3}{\gamma_1 \leq \gamma_3}$$

$$\frac{\gamma_1 \leq \gamma_2 \quad S^t \leq R^{t'}}{\text{ch}(\gamma_1)@S^t \leq \text{ch}(\gamma_2)@R^{t'}}$$



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∴ Outputs may grow  
Inputs may shrink

## ⑥ Typing names

$$\Gamma \vdash_s n : \gamma$$

- △ if  $n$  is a simple name, then it belongs to  $s$

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## ⑥ Typing processes

$$\Gamma \vdash_{s,S} P$$

- △ simple names of  $P$  considered of  $s$
- △ at runtime,  $P$  might be in any site of  $S$

## ⑥ Example

$$s_G \mathbf{[} a?(x : \{r, t\}) x?(\dots) \mathbf{]}_{S=\{r,t\}} P$$

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## ⑥ Typing networks

$$\Gamma \vdash N$$

# Typing located outputs

## ⑥ Rule

$$\frac{\begin{array}{c} \Gamma \vdash_s v : \gamma_2 \\ \gamma_2 \leq \gamma_1 \\ \Gamma(r)_1(a) = \text{ch}(\gamma_1)@ \{r\}^b \\ S \subseteq \Gamma(r)_2(\text{rem}) \end{array}}{\Gamma \vdash_{s,S} a@r! \langle v \rangle}$$

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# Typing located inputs

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$$\frac{\begin{array}{c} \Gamma \vdash_{s, \{r\}} P \\ \Gamma(r)_1(a) = \text{ch}(\gamma_1) @ \{r\}^b \\ \Gamma(s)_1(x) = \text{ch}(\gamma_2) @ R^b \\ \text{ch}(\gamma_2) @ R^b \leq \gamma_1 \\ S \subseteq \Gamma(r)_2(\text{mig}) \end{array}}{\Gamma \setminus x@s \vdash_{s,S} a@r?(x : R) P}$$

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## ⑥ Example

$$s_\emptyset \mathbf{[} a@r?(x : \{t\}) x! \langle c \rangle \mathbf{]} \parallel r_{\{\text{mig}:\{s\}\}} \mathbf{[} a! \langle b@t \rangle \mathbf{]} \parallel t_{\{\text{rem}:\{r\}\}} \mathbf{[} 0 \mathbf{]}$$

# Typing located names (nets)

---

## ⑥ Rule

$$\Gamma \vdash N$$

$$S \setminus s \subseteq \Gamma(s)_2(\text{new})$$

$S$  is the set of sites where  $a@s$  occurs free in  $N$

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$$(\nu a@s) \mathcal{S}_{\{\text{new}:\{r\}, \text{rem}:\{r\}\}} \mathbf{[0]} \parallel r_\emptyset \mathbf{[a@s! \langle b \rangle]}$$

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$$S = \{r\}$$

$$\Gamma(s) = \{(\emptyset, \{\text{new} : \{r\}, \text{rem} : \{r\}\})\}$$

$$\Gamma(r) = \{(b : \text{ch}(\gamma)@ \{r\}^b, \emptyset)\}$$

# Runtime errors

$$\mathcal{E} = \{N \mid N \rightarrow^* \nu \vec{X}(M' \parallel M)\}$$

and  $M$  of the form

## ⑥ Remote communication

$$\begin{array}{ll} r_{G_1}[P] \parallel s_{G_2}[a@r! \langle v \rangle], & s \notin G_1(\text{rem}) \\ s_G[a! \langle b@r \rangle \mid a?(x : S) P], & r \notin S \end{array}$$

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## ⑥ Migration

$$r_{G_1}[P] \parallel s_{G_2}[a@r?(x : S) P], \quad s \notin G_1(\text{mig})$$



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## ⑥ Migration

$$r_{G_1}[P] \parallel s_{G_2}[a@r?(x : S) P], \quad s \notin G_1(\text{mig})$$

## ⑥ Name creation

$$r_{G_1}[P] \parallel s_{G_2}[(\nu a@r) P], \quad s \notin G_1(\text{new})$$

# *The usual properties*

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## ⑥ Subject reduction

if  $\Gamma \vdash N$  and  $N \rightarrow M$ , then  $\Gamma \vdash M$

## ⑥ Well-typed networks free of runtime errors

if  $\Gamma \vdash N$  and  $N \rightarrow^* M$ , then  $M \notin \mathcal{E}$

# *Conclusions and further work*

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  - △ Sites are constants (used explicitly in types!)
- ⑥ Further work
  - △ Solve the above limitations :))
  - △ Specify security policies at channel level
  - △ Adjust security policies dynamically